



DEVELOPMENT OF INTERACTIVE SOFTWARE FOR SIMULATION OF MATERIAL AND WAVE PROPERTIES OF PIEZOELECTROMAGNETICS INCORPORATING GRAVITATIONAL PHENOMENA

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ABSTRACT

This short report acquaints the reader with the developed software that can work with pure piezoelectrics, pure piezomagnetism, pure piezoelectromagnetics (PEMs), and the PEMs with incorporation of gravitational phenomena, i.e. piezo gravito torsion electromagnetic (PGTEM) materials. This software can calculate the material properties and wave characteristics in all the aforementioned continuous media. Also, it allows the PEM and PGTEM composite creation from the material parameters of both piezoelectrics and piezomagnetism that present in the software database or can be loaded from a file. The interface of the developed interactive software and sample calculations are demonstrated.

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Keywords: Software developing, simulation of material and wave properties, magnetoelectric and gravitational effects, acoustic wave propagation, piezoelectromagnetics.

INTRODUCTION

The theory on the acoustic wave propagation coupled with the electrical, magnetic, gravitational, and torsional (i.e. cogravitational) potentials was developed by Zakharenko (2016) and (2017a). Some mathematical problems were resolved in (Zakharenko, 2018a). It was found that these four-potential shear-horizontal (4P-SH) acoustic waves can propagate along the surface of the suitable solid (Zakharenko, 2016), along the common interface between two dissimilar solids (Zakharenko, 2017b) and in plates (Zakharenko, 2018b).

All the obtained speeds of the different 4P-SH acoustic waves depend on the material parameter called the coefficient of the electromagnetogravitotorsionomechanical coupling (CEMGTC) discussed in (Zakharenko, 2018c). In the solids, these acoustic wave speeds can also depend on the speeds of the electromagnetic and gravitational (namely gravitotorsional) waves, and two faster speeds. These two fast speeds can exist in solids and a vacuum. Therefore, these fast waves can be used for instant interplanetary (interstellar and even intergalactic) communications. Review by Zakharenko (2020) has combined evaluations of propagation speeds of gravitational phenomena in continuous media that was done from Newton's time to this century because Newton's theory of gravitation assumes an instant speed for gravitational phenomena. Some suggestions concerning the instant interplanetary

communication were introduced in (Zakharenko, 2018d). For this purpose, the development of proper infrastructure on the Earth is necessary. It is obvious that the successful development can be based on resolving many theoretical, mathematics, experimental, and engineering problems.

First of all, it is necessary to investigate these problems for solid continua. Then, it is possible to use obtained experience for a vacuum. However, acoustic waves cannot propagate in a vacuum. To study the acoustic wave propagation in the piezoelectromagnetic (i.e. magnetoelectric) materials with taking into account the gravitational phenomena, i.e. the piezogravitotorsionoelectromagnetic (PGTEM) materials, is significantly more complicated in comparison with the purely piezoelectromagnetic case. As a result, many material parameters must be taken into account for calculation of wave parameters. To put forward investigations of these PGTEM (composite) materials, the interactive software was created at the International Institute of Zakharenko Waves (IIZWs, www.iizw.ru).

The following section introduces the developed software. This software deals with all the aforementioned materials because the study of the PGTEM materials requires this peculiarity. For this aim, it is necessary to use existing or created piezoelectrics, piezomagnetism, and piezoelectromagnetics, as well as auxiliary piezogravitics, piezotorsionics, and piezogravitotorsionics in order to create a PGTEM material with desired properties.

Description

The created software (first version) written with the free Lazarus tools can be downloaded here: https://www.researchgate.net/publication/338517269_On_evaluations_of_fast_speeds_of_propagation_of_gravitational_phenomena_A_review as a file.zip that contains the single file.exe (~ 10 MB) for installation on a Windows 7/8/10 computer. For installation, it requires only ~ 60 MB of the hard disk space and can be uninstalled similar to any other software. After installation, the main form shown in Figure 1 starts. This form has two TabSheets shown in Figures 1 and 2, respectively.

For user reference, the first TabSheet provides the vacuum parameters just below the main title. The electric, magnetic, gravitic constants and the speed of light can be found in the reference book on physics (Yavorsky *et al.*, 2006). Using the gravitic constant and the speed of light, the torsionic constant can be calculated. The other vacuum parameters in Figure 1 have the evaluated values borrowed from (Zakharenko, 2017b, 2018a, 2018c). For convenience, all the vacuum parameters have their physical dimensions. These vacuum parameters are used in suitable calculations of speeds of the acoustic waves propagating in the solids when there is a coupling with a vacuum. Below the vacuum parameters there are dialogs for selection of suitable materials. First of all, it is necessary to choose the crystal symmetry, hexagonal or cubic. Each crystal symmetry loads its own default list of material parameters for piezoelectrics, piezomagnetism, piezoelectromagnetics, piezogravitics, piezotorsionics, and piezogravitotorsionics. As soon as the user has chosen any of the aforementioned materials the results of the calculations are shown in two output areas located at bottom-right of the main form shown in Figure 1.

For the piezogravitotorsionoelectromagnetic (PGTEM) materials there is the second TabSheet of the main form shown in Figure 2. On the left it has two dialogs for comparison of the material parameters of any pair of the PGTEM materials. Also, the left and right PGTEM materials can be moved to the right dialog for corrections of the values of the PGTEM material by pushing the buttons called "PGTEM1" and "PGTEM2" with arrows, respectively. The calculated material and wave parameters are shown in two output columns situated between two groups of buttons.

The group of three buttons on the bottom-right allows the user to add, load, and save any desired PGTEM material with the material parameters located in the fields above these buttons up to the crystal symmetry. So, the user can save the PGTEM parameters to a text file, open a text file containing the material parameters created by the user, and add the loaded (created, corrected) PGTEM

parameters to the common list of the PGTEMs. The output form with figures and calculated data shown in Figure 3 is created as soon as the user pushes on one of the left-group buttons.

In the appeared output form shown in figure 3 there are two figures and several columns of output data. All these data can be saved to a file by pushing the single button on the top-right. The output form has two TabSheets with output data for the PGTEM materials. The second TabSheet is not shown here due to the page limitation for the conference proceedings. The same output form, for instance, for a piezoelectrics is appeared when the user pushes the button entitled "Calculate" situated on the other form that is called when the user pushes the longest button on the bottom of the main form shown in Figure 1. For piezoelectrics, however, the output form contains only the single TabSheet with the corresponding data shown in Figure 3. This is due to the fact that piezoelectrics possess a small number of the input and output data in comparison with the piezoelectromagnetics and the PGTEM materials.

Pushing the button entitled "Create PEMs, PGs, PTs, PGTs" (Fig. 1) causes the creation of one piezoelectromagnetics, four piezogravitics, four piezotorsionics, sixteen piezogravitotorsionics, and sixteen PGTEM composite materials. They are immediately available in the corresponding listings for calculation for their properties. This procedure if the composite materials' creation is useful because the difference in the values of some material parameters can reach forty orders in this case. However, the software was successfully tested on Windows 7 and 10 platforms in various countries. The software has demonstrated its stability and correctness.

The button entitled "Show References" (Fig. 1) is for loading of one extra form that contains the references for the piezoelectrics, piezomagnetism, piezoelectromagnetics, etc. This form also contains the other information and a short instruction for the user.

For instance, for the pure piezoelectrics present in the IIZWs software there are the following default crystals: piezoelectrics PZT-7A (hexagonal symmetry class 6 *mm*) (Yang, 2000; Jaffe and Berlincourt, 1965), PZT-5H (6 *mm*) (Pak, 1992), CdSe (6 *mm*) (Sharma *et al.*, 2005), ZnO (6 *mm*) (Su *et al.*, 2005), Bi₁₂SiO₂₀ (cubic symmetry class 23) (Kamenov *et al.*, 2000), Bi₁₂GeO₂₀ (23) (Zakharenko, 2011), Bi₁₂TiO₂₀ (23) (Zakharenko, 2007), Ti₃TaSe₄ and Ti₃VS₄ (cubic Chalcogenides, $\bar{4}3m$) (Henaff, 1982), β -ZnS ($\bar{4}3m$) (Zakharenko, 2010a) etc.

Main Input Window Created PGTEM Composites
International Institute of Zakharenko Waves (IZW), www.izw.ru

Calculation of propagation speeds of acoustic waves for piezoelectromagnetic materials incorporating gravitational phenomena

Parameters

Electric constant [F/m]: for a vacuum: 0.088541878128E-10	Gravitic constant [kgF/m ²]: 1.498287880967544334E+10	Electromagnetic constant [s/m]: 1.0E-14	Gravitatorsonic constant [s/m]: 2.0E-14	Torsionomagnetic constant [m/C]: 1.0E-02	Gravotomagnetic constant [WbF/m ²]: 1.0E-02
Magnetic constant [N/A ²]: 1.256637061435917295E-6	Torsionic constant [m/kg]: 0.0742614333054188E-26	EM-exchange speed, Va0 [m/s]: 1.000000000000000E+14	GT-exchange speed, Vs0 [m/s]: 5.000000000000000E+13	Torsioelectric constant [CF/m ²]: 1.0E-07	Torsioelectric constant [m/Wb]: 1.0E-40
Speed of light [m/s]: 2.99792458081606E+08	Speed of light with a0 [m/s]: 2.99792458082954E+08	Speed of light with s0 [m/s]: 2.99792458086995E+08	Speed of light with s0 [m/s]: 2.99792458086995E+08	Speed of first fast wave [m/s]: 1.000000000000000E+21	Speed of second fast wave [m/s]: 1.000000000000000E+21

Crystal symmetry: Hexagonal

Piezoelectrics (PEs): PZT-7A (6 mm)

Parameter:	Value:
Ro =	7.500E+03
C44 = C66 =	2.540E+10
e16 = e34 =	9.200E+00
d11 = d33 =	42.50E-10
m11 = m33 =	0

Piezomagnetism (PMs): Terfenol-D (Tb2Dy73Fe195, 6 mm)

Parameter:	Value:
Ro =	9.060E+03
C44 = C66 =	0.850E+10
h16 = h34 =	112.50E+00
d11 = d33 =	0
m11 = m33 =	3.080E-06

Piezoelectromagnetics (PEMs): (6 mm)_Terfenol-D (Tb27Dy73Fe195, 6 mm)

Parameter:	Value:
Ro =	8.280000000000E+03
C44 = C66 =	1.695000000000E+10
e16 = e34 =	6.5038238691624
h16 = h34 =	79.5495128834866
d11 = d33 =	42.50E-10
m11 = m33 =	3.080E-06
a11 = a33 =	1.14411537880E-08

Piezogravitatorsonics (PGTs): cPGTs_1_1_PZT-7A (6 mm)_Terfenol-D (Tb271)

Parameter:	Value:
Ro =	8.280000000000E+03
C44 = C66 =	1.695000000000E+10
g16 = g34 =	13794294504.6891
f16 = f34 =	1.77654465620036E-9
p11 = p33 =	1.49828788097E+11
n11 = n33 =	0
s11 = s33 =	7.42614333054E-27
t11 = t33 =	3.33564095108E-09

Piezotorsionics (PTs): cPTs_1_1_Terfenol-D (Tb27Dy73Fe195, 6 mm)

Parameter:	Value:
Ro =	9.060E+03
C44 = C66 =	0.850E+10
f16 = f34 =	2.51241354696E-09
p11 = p33 =	0
n11 = n33 =	7.42614333054E-27

Output Material Parameters:

b10 =	-0.003225461975880
b11 =	0.058169331304731
b12 =	0.339930140004014
b13 =	-0.040250124208736
b14 =	0.010520740207861
b15 =	-0.351878691022860
b16 =	0.37645207504370
b17 =	0.397350024158837

Output Waves' Speeds:

Vnew8 =	1579.9141546170
Vnew9 =	172.5204202296
Vnew10 =	1844.4822076995
Vnew11 =	1841.3685813725
Vnew12 =	1734.6535878738
Vnew13 =	1842.9970915544
Vnew14 =	1844.3897198953
Vnew15 =	1726.5284570860
Vnew16 =	1708.8034556417
Vnew17 =	1692.6294951280

Show References

Create PEMs, PGs, PTs, PGTs

Input/Compare/Save/Delete of PEs, PMs, PEMs, PGs, PTs, PGTs

Fig. 1. The main form that starts as soon as this software is installed on a Windows 7/8/10 computer.

Calculation of propagation speeds of acoustic waves for piezoelectromagnetic materials incorporating gravitational phenomena

Created PGTEM Composite Material Parameters:

Crystal Symmetry: Hexagonal

List of PGTEM Composites: cPGTEMs_1_1_PZT-5H (6 mm)_Terfenol-D (Tl) (6 mm)_Terfenol-D (Tb27D7BFeL95, 6 mm)

Created PGTEM Composite:

Parameter:	Value:
Ro =	8.405000000000E+03
C44 = C66 =	2.190000000000E+10
e16 = e24 =	12.0208152801713
h16 = h34 =	79.549512834866
g16 = g34 =	16.261851401.0777
f16 = f34 =	1.77654465620036E-9
d11 = d33 =	151.0E-10
m11 = m33 =	3.080E-06
p11 = p33 =	1.49828788097E-11
n11 = n33 =	7.42614333054E-27
a11 = a33 =	2.15657135287E-08
s11 = s33 =	3.33564095108E-09
l11 = l33 =	1.51236640594E-18
Z11 = Z33 =	4.75648473167E-01
B11 = B33 =	6.79317795541E+00
K11 = K33 =	1.05893703444E-19

Output Material Parameters:

M54 = 5.07005948464E-27
M5 = 5.07005948464E-27
A10 = 5.67344311623E-17
A1 = 5.67344311623E-17
A2 = 1.11034302714E-16
Kemt2 = 0.5109630968
bBGpe = 0.304088890759485
bBGpm = 0.085770049860989
bBGpg = 0.015863029703875
bBGpt = 0.00386627458486
bBGMem = 0.35211036180611
bBGMgt = 0.01826435869341
bnewl = 0.338170467473602

Output Waves' Speeds:

Clg = 2.99792458081606E-08
Vemgt = 1984.1757030602
Vfast1 = 3.72845096300E-08
Vfast2 = 3.72845096300E-08
Vfast0 = 1.000000000E-21
Vfast02 = 1.000000000E-21
VBGpe = 1843.345753410
VBGpm = 1681.9850348857
VBGpg = 1626.9371504257
VBGpt = 1617.3020243033
VBGMem = 1862.4158251617
VBGMgt = 1628.858897677
Vnewl = 1867.2773360867

Calculate PGTEM SH-SAWS

Calculate PGTEM SH-Acoustic Waves in Plate

Calculate Interfacial PGTEM SH-Acoustic Waves for Two Dissimilar Materials

Fig. 2. The second TabSheet of the main form that contains all the input and output data of the created PGTEMs materials.

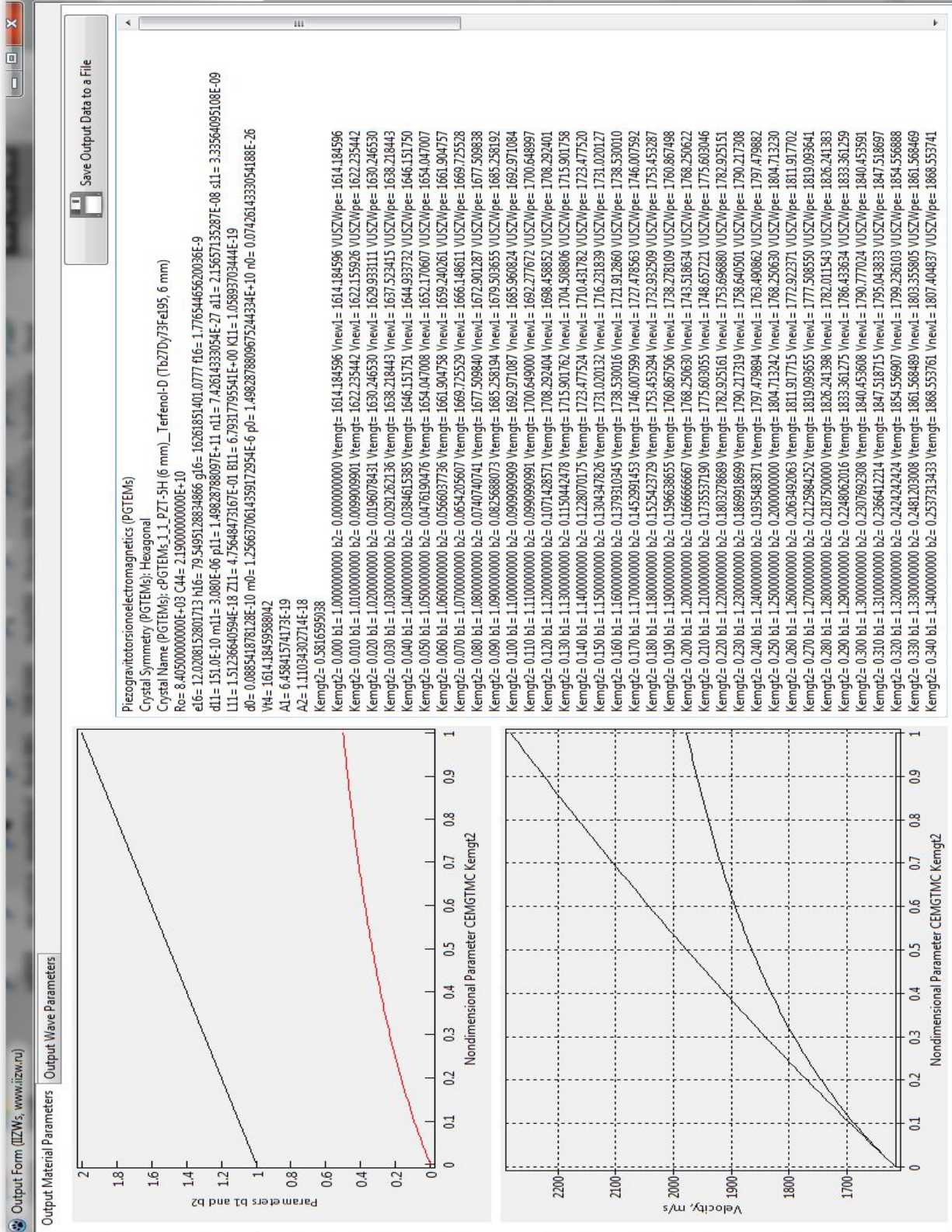


Fig. 3. The output form with figures and input and output data that is created when the user pushes the button called “Calculate PGTEM SH-SAWs” located on the second TabSheet of the main form.

Of the purely piezomagnetic materials there are CoFe_2O_4 (6 mm) (Zhou *et al.*, 2012; Annigeri *et al.*, 2006; Aboudi, 2001; Liu and Chue, 2006), Terfenol-D ($\text{Tb}_{27}\text{Dy}_{73}\text{Fe}_{195}$, 6 mm) (Giannakopoulos and Parmaklis, 2007), CoFe_2O_4 (m3m) (Srinivas *et al.*, 2006; Ramirez *et al.*, 2006)[25, 26], Alfenol ($\text{Fe}_{90}\text{Al}_{10}$, m3m) (Avellaneda and Harshe, 1994), Galfenol ($\text{Fe}_{81}\text{Ga}_{19}$, m3m) (Zakharenko, 2010b), Metglas 2605 (FeBSiC , m3m) (Zhai *et al.*, 2006), YIG ($\text{Y}_3\text{Fe}_5\text{O}_{12}$, m3m) (Fiebig, 2005), NiFe_2O_4 and Ni (m3m) (Zakharenko, 2012; Kaczkowski, 1970), etc.

It is natural that the created software can be further developed in the future concerning some improvements in the design and creation of extra output data for PGTEM materials. The theoretical developments in this research arena will also result in extra calculations of the material and wave parameters that can be added in the software.

CONCLUSION

It is demonstrated the developed software that allows the reader to calculate the material and wave characteristics for pure piezoelectrics, pure piezomagnetics, pure piezoelectromagnetics, and the piezogravitotorsionoelectromagnetics. This interactive software will also allow the creation of new PEM and PGTEM composites with desired properties and to record all the obtained results to a file. The figures graphically demonstrated the software interface and sample calculations of some material and wave parameters.

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